

## UNIT-3: Quadratic Equations and Inequalities

- Q.1** If  $\alpha, \beta$  are the root of a quadratic equation  $x^2 - 3x + 5 = 0$  then the equation whose roots are  $(\alpha^2 - 3\alpha + 7)$  and  $(\beta^2 - 3\beta + 7)$  is  
 (A)  $x^2 + 4x + 1 = 0$  (B)  $x^2 - 4x + 4 = 0$   
 (C)  $x^2 - 4x - 1 = 0$  (D)  $x^2 + 2x + 3 = 0$
- Q.2** If  $\alpha, \beta$  are root of the equation  $x^2 - 5x + 6 = 0$  then the equation whose roots are  $\alpha + 3$  and  $\beta + 3$  is  
 (A)  $x^2 - 11x + 30 = 0$  (B)  $(x-3)^2 - 5(x-3) + 6 = 0$   
 (C) Both (A) and (B) (D) none
- Q.3** If  $a, p, q$  are non-zero real numbers, the two equations  $2a^2x^2 - 2abx + b^2 = 0$  and  $p^2x^2 + 3pqx + q^2 = 0$  have  
 (A) No common root  
 (B) One common root if  $2a^2 + b^2 = p^2 + q^2$   
 (C) Two common roots if  $3pq = 2ab$   
 (D) Two common roots iff  $3qb = 2ap$
- Q.4** If  $a > b > 0$  are two real numbers, the value of  $\sqrt{ab+(a-b)}\sqrt{ab+(a-b)}\sqrt{ab+(a-b)}\sqrt{ab+\dots}$  is  
 (A) Independent of  $b$  (B) Independent of  $a$   
 (C) Independent of both  $A$  and  $B$   
 (D) Dependent on both  $A$  and  $B$
- Q.5** The equation  $x^2 + (1 + 2\sin\theta)x + \sin 2\theta(\sin\theta - \cos\theta) = 0$  has roots of equal magnitude but opposite signs for  
 (A) Only one value of  $\theta$  (B) Only two values of  $\theta$   
 (C) Infinitely many values of  $\theta$  (D) No value of  $\theta$
- Q.6** The number of solutions of the equation  $4x(x-3) - 5|2x-3| + 13 = 0$  is  
 (A) 1 (B) 2 (C) 3 (D) 4
- Q.7** The quadratic expression  $21 + 12x - 4x^2$  are  
 (A) The least value 5 (B) The highest value 30  
 (C) The highest value 21 (D) None of these
- Q.8** The roots of  $x^2 - 8|x| + 12 = 0$   
 (A) Do not form a progression  
 (B) Form an A.P. with Zero sum  
 (C) Form an A.P. with non-zero sum  
 (D) Form a G.P.
- Q.9** The quadratic equation with real coefficients one of whose complex roots has the real part 12 and modulus 13 is  
 (A)  $x^2 - 12x + 13 = 0$  (B)  $x^2 - 24x + 13 = 0$   
 (C)  $x^2 - 24x + 169 = 0$  (D)  $x^2 - 24x - 13 = 0$
- Q.10** The quadratic equation  $(3 + \sin\theta)x^2 + (2\cos\theta)x + 2 - \sin\theta = 0$  has  
 (A) Equal roots for all  $\theta$   
 (B) Real and distinct roots for all  $\theta$   
 (C) Complex roots for all  $\theta$   
 (D) Real or complex roots depending upon  $\theta$
- Q.11** If  $a, b, c$  are real and  $a \neq b$ , then the roots of the equation  $2(a-b)x^2 - 11(a+b+c)x - 3(a-b) = 0$  are -  
 (A) real and equal (B) real and unequal  
 (C) purely imaginary (D) none of these
- Q.12** The quadratic expression  $21 + 12x - 4x^2$  takes -  
 (A) the least value 5 (B) the greatest value 30  
 (C) the greatest value 21 (D) none of these
- Q.13** If  $\sin^x\theta + \cos^x\theta \geq 1, 0 < \theta < \pi/2$ , then -  
 (A)  $x \in (-\infty, 2]$  (B)  $x \in [-2, 2]$   
 (C)  $x \in [-1, 1]$  (D)  $x \in [2, \infty]$
- Q.14** The number of positive terms in the expansion of  $(1 - 2x + x^2)^n (1 + x + x^2)^{2n}, x > 0$  and  $n \in \mathbb{N}$  is  
 (A)  $n$  (B)  $n + 1$   
 (C)  $2n + 1$  (D)  $(n + 1)(2n + 1)$
- Q.15** If  $\sin x + \cos x = \sqrt{y + \frac{1}{y}}, x \in [0, \pi]$ , then  
 (A)  $x = \pi/4$  (B)  $x = \pi/2$   
 (C)  $x = \pi/3$  (D)  $x = 3\pi/4$
- Q.16** The inequalities  $y(-1) \geq -4, y(1) \leq 0$  and  $y(3) \geq 5$  are known to hold for  $y = ax^2 + bx + c$  then the least value of 'a' is  
 (A)  $-1/4$  (B)  $-1/3$   
 (C)  $1/4$  (D)  $1/8$

## UNIT-3: Quadratic Equations and Inequalities

- Q.17** If the roots of the equation,  $\frac{1}{x+p} + \frac{1}{x+q} = \frac{1}{r}$  are equal in magnitude but opposite in sign then  $p+q$  is equal to  
 (A)  $r$  (B)  $2r$   
 (C)  $(1/2)r$  (D) none of these
- Q.18** The roots of the equation  $x^2 - 2\sqrt{2}x + 1 = 0$  are (2010)  
 (A) Real and different (B) Imaginary and different  
 (C) Real and equal (D) Rational and different
- Q.19** If  $p$  and  $q$  are roots of the equation  $x^2 - 2x + A = 0$  and  $r$  and  $s$  be roots of the equation  $x^2 - 18x + B = 0$  if  $p < q < r < s$  be in A.P., then  $A$  and  $B$  are respectively –  
 (A)  $-3, 77$  (B)  $3, 77$   
 (C)  $3, -77$  (D) none of these
- Q.20** If the roots of equation  $x^2 + bx + ac = 0$  are  $\alpha, \beta$  and roots of the equation  $x^2 + ax + bc = 0$  are  $\alpha, \gamma$  then the value of  $\alpha, \beta, \lambda$  respectively –  
 (A)  $a, b, c$  (B)  $b, c, a$   
 (C)  $c, a, b$  (D) none of these
- Q.21** If the quadratic equations  $ax^2 + 2cx + b = 0$  and  $ax^2 + 2bx + c = 0$  ( $b \neq c$ ) have a common root, then  $a + 4b + 4c$  is equal to –  
 (A)  $-2$  (B)  $-1$   
 (C)  $0$  (D)  $1$
- Q.22** The value of  $m$  for which one of the roots of  $x^2 - 3x + 2m = 0$  is double of one of the roots of  $x^2 - x + m = 0$  is  
 (A)  $0, 2$  (B)  $0, -2$   
 (C)  $2, -2$  (D) none of these
- Q.23** If the expression  $x^2 - 11x + a$  and  $x^2 - 14x + 2a$  must have a common factor and  $a \neq 0$ , then, the common factor is –  
 (A)  $(x-3)$  (B)  $(x-6)$  (2009)  
 (C)  $(x-8)$  (D) none of these
- Q.24** If the roots of the equation  $x^2 + 3x + 2 = 0$  and  $x^2 - x + \lambda = 0$  are in same ratio then the value of  $\lambda$  is given by-  
 (A)  $2/7$  (B)  $2/9$   
 (C)  $9/2$  (D)  $7/2$
- Q.25** The sum of all real roots of the equation  $|x-2|^2 + |x-2| - 2 = 0$ , is –  
 (A)  $0$  (B)  $8$   
 (C)  $4$  (D) none of these
- Q.26** The minimum value of  $f(x) = x^2 - 2bx + 2c^2$  is more than the maximum value of  $g(x) = -x^2 - 2cx + b^2$ ,  $x$  being real, for –  
 (A)  $|c| < |b|\sqrt{2}$  (B)  $0 < c < b\sqrt{2}$   
 (C)  $|c| > |b|\sqrt{2}$  (D)  $b\sqrt{2} < c < 0$
- Q.27** If the roots of  $x^2 - bx + c = 0$  are two consecutive integers, then  $b^2 - 4c$  is –  
 (A)  $0$  (B)  $2$  (C)  $3$  (D)  $1$
- Q.28** If  $a, b, c$  are non-zero real numbers, then two equations  $2a^2x^2 - 2abx + x^2 = 0$  and  $ax^2 + bx - c^2 = 0$  have –  
 (A) no common root (B) two common roots  
 (C) one common root if  $a > 0$  (D) no common root if  $a > 0$
- Q.29** Let  $a, b, c \in \mathbb{R}$  and  $ax^2 + bx + c = 0$  has two negative roots, then – (2008)  
 (A)  $a, b, c$  are of same sign (B)  $a, -b, c$  are of same sign  
 (C)  $a, b, -c$  are of same sign (D)  $a, -c$  are of same sign
- Q.30** The equation  $\pi^x = -2x^2 + 6x - 9$  has –  
 (A) one solution (B) two solutions  
 (C) infinite solutions (D) no solution
- Q.31** Number of integral values of  $x$  satisfying the inequality  $\left(3^{\frac{5}{2} \log_3(12-3x)}\right) - \left(3^{\log_2 x}\right) > 32$  are .....  
 (A)  $2$  (B)  $6$  (C)  $8$  (D)  $10$
- Q.32**  $\frac{8x^2 + 16x - 51}{(2x-3)(x+4)} > 3$ , if  $x$  satisfies  
 (A)  $x < -4$  (B)  $-3 < x < 3/2$   
 (C)  $x > 5/2$  (D) all the above
- Q.33** Number of solution for the system of inequalities  $\begin{cases} 2x+1 < x+2, \\ x-1 > 2x \end{cases}$  (2007)  
 (A)  $1$  (B)  $2$  (C)  $3$  (D)  $0$
- Q.34** Solution for the system of inequalities:  $\begin{cases} x^2 - 3x + 2 \geq 0 \\ x - x^2 + 2 \geq 0 \end{cases}$   
 (A)  $[-1, 1] \cup \{2\}$  (B)  $[1, 1] \cup \{2\}$   
 (C)  $[1, -1] \cup \{2\}$  (D)  $[-1, -1] \cup \{2\}$